49 Maths Knowledge Organiser Topic 14: Quadratic Functions

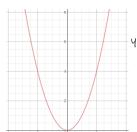
What must I be able to do?	Key vocabulary	
New content: Sketch graphs of quadratic functions, considering orientation and labelling the point of intersection with the y axis, considering what happens to y for large positive and negative values of x	Quadratic function	An equation where the <u>highest</u> <u>power</u> of a variable (usually x) <u>is 2</u> , e.g. it contains an x² power but not an x³ or higher. We use both the word function and equation to mean the same thing here.
 □ Find approximate solutions of a quadratic equation from the graph of the corresponding function ▶ Sparx U989, U667 	Roots	The values of x in a quadratic equation which give a value of y = 0. On a graph, this is where it crosses the x-axis.

General form of a quadratic equation

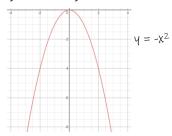
The general equation of a quadratic is $y = ax^2 + bx + c$, where a, b and c are all constant values. The +c represents the intercept and tells us where the graph will cross the y-axis.

If the a is positive, the graph will form a u shape.

If the a is negative the graph will form a n shape.



The graph is a smooth curve between each point and is called a parabola.



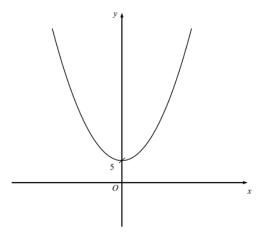
Sketching quadratics

All you need to know is whether it forms a u or a n shape, and identify where it would cross the y-axis.

e.g. sketch the graph $y = 3x^2 + 5$

a = 3 so is positive. So this is a u shape

c = 5, so crosses at (0, 5)



As it is a sketch, there is no need to plot any points accurately. The graph should be symmetrical about the y-axis and just label the crossing point.

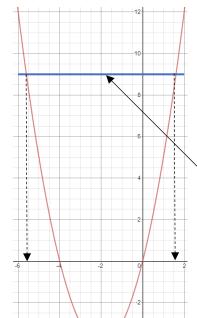
Plotting and using quadratic graphs

e.g. a) Complete the table of values for $y = x^2 + 4x$ and plot the graph

Χ	-6	-4	-2	O	2
Ч	12	D	-4	D	_12

 $y = (-6)^2 + 4 \times -6$ y = 36 - 24 = 12

Às a quadratic graph is symmetrical, you will often see repeating values of y



b) Use the graph to find estimates for the solutions of $x^2 + 4x = 9$

We already have the graph of $y = x^2 + 4x$

We draw on to the same axis the graph of

y = 9

Where the 2 graphs intersect (cross) we read off the two x values.

So x = 1.5 and x = -5.5